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Kumamoto University
Temperature Dependence of the Second-order Elastic Constants of AgBr

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The temperature dependence of the second-order elastic constants of AgBr is calculated by using a thermodynamic relation. It is shown that the model reproduces the experimental values of the elastic constant $C_{44}$ from room temperature to near the melting point. However, the calculated values of $C_{11}$ and $C_{12}$ are estimated over the experimental data by large amounts above 550 K. The result indicates that in the case of AgBr, the material parameters evaluated at the reference temperature (room temperature) can not be extrapolated above 550 K and that the model for the elastic constant used widely in the literature should be used carefully.

§1. Introduction

It is well known that AgCl and AgBr have the NaCl structure. However, their lattice dynamical properties are much different from those of alkali halides. For example, compared to alkali halides, the Ag halides have low melting points, high dielectric constants, high ionic conductivities, high thermal expansion coefficients, etc. In particular, it is well known that AgI shows superionic conductivity in the temperature range $T_c < T < T_m$, where $T_c = 420$ K is the superionic transition temperature and $T_m = 831$ K is the melting temperature. The superionic conducting phase has been frequently described as a sublattice melted phase. AgI has a wurtzite or zinc blende structure at room temperature and ambient pressure. At $T_c$ it transforms to the superionic conducting phase in which the I$^-$ ion sublattice takes an fcc structure and the Ag$^+$ ions are distributed among the many available sites provided by the I$^-$ sublattice. Concerning the origin of superionic behavior, the bond fluctuation model has been proposed. According to this model, the fast ion movement in solids occurs accompanied by local change of the bonding. Regarding the parent compounds AgBr and AgCl, they are not usually classified as superionic conductors. However, these materials exhibit also high ionic conductivity and their lattice dynamical properties are sufficiently anomalous as in the case of AgI.

In the present report, the temperature dependence of the elastic constant of AgBr is examined based on a thermodynamic relation. Study on the behavior of elastic constant is important, because it provides useful information concerning cohesive energy and interatomic interaction of the materials. The result of our analysis reveals that the relation widely used in the literature does not describe adequately the temperature dependence of the elastic constants of AgBr. In cubic crystals, there are three independent elastic constants, $C_{11}$, $C_{12}$ and $C_{44}$. These elastic constants describe the longitudinal, transverse and shear stiffness, respectively.
§2. Temperature dependence of elastic constants

The Anderson-Grüneisen parameter which is used widely in the discussion of elastic properties of solids is given by

\[ \delta_T = -\frac{1}{\alpha K_T} \left( \frac{\partial K_T}{\partial T} \right)_P, \]  

(2.1)

where \( \alpha \) is the thermal expansion coefficient and \( K_T \) is the isothermal bulk modulus. By using the definition of the thermal expansion coefficient, the above equation becomes

\[ \delta_T = -\frac{V}{K_T} \left( \frac{\partial K_T}{\partial V} \right)_P. \]  

(2.2)

Some years ago, it was shown that Eq. (2.2) can be generalized as

\[ \delta_M = -\frac{V}{M} \left( \frac{\partial M}{\partial V} \right)_P, \]  

(2.3)

where \( M \) is any of the elastic moduli such as bulk modulus and elastic constants.

Among various equations of state for solids proposed till now, the equation of Murnaghan is one of the most widely used. In the framework of Murnaghan's equation, the quantity \( \delta_M \) defined in Eq. (2.3) is assumed to take a constant value. Under this assumption, the elastic modulus can be written as

\[ M(T) = M_0 \left( \frac{V(T)}{V_0} \right)^{-\delta_M}, \]  

(2.4)

where the suffix 0 denotes the quantities taken at the temperature of reference. In the past, Eq. (2.4) was used to analyze the temperature dependence of the elastic constants of ionic solids such as NaCl, KCl, MgO, etc. These studies revealed that Eq. (2.4) reproduces quite well the behavior observed experimentally over wide range of temperatures. Eq. (2.4) was also applied to study the temperature dependence of the elastic constant of AgCl. There, it was shown that the agreement between the calculated and the measured data are good for \( C_{11} \) and \( C_{12} \). However, concerning \( C_{44} \), a deviation was observed at high temperature. This result motivated us to apply Eq. (2.4) to study the temperature dependence of the elastic constant of AgBr.

§3. Results and discussion

Figures 1 – 3 show the temperature dependences of the elastic constants \( C_{11} \), \( C_{12} \) and \( C_{44} \) of AgBr. The solid line represents the calculated curve by Eq. (2.4) and the circles are the experimental data.
Fig. 1. The temperature dependence of the elastic constant $C_{11}$ of AgBr.

Fig. 2. The temperature dependence of the elastic constant $C_{12}$ of AgBr.
Contrary to the result reported for AgCl, the agreement between the measured and calculated values is good for $C_{44}$ as shown in Fig. 3. Concerning $C_{11}$ and $C_{12}$, large deviations are apparent above 550 K as shown in Figs. 1 and 2, respectively. Comparing with the case of AgCl, the degree of deviation from the theoretical prediction is larger in AgBr. We note that the theoretical curve is evaluated over the values of $C_{11}$ and $C_{12}$ above 550 K. This means that there is a softening in the elastic constants of the crystals above 550 K and that the material parameters evaluated at the reference of room temperature cannot be used at high temperatures. In silver halides, it is well documented that the concentration of Frenkel defects increases dramatically at high temperatures. Therefore, a part of the large deviations observed in $C_{11}$ and $C_{12}$ is caused undoubtedly by these defects. In the microscopic theory of elastic constants, the effect of these defects should be included. In the phenomenological theory as used in our analysis, the effect of defects enters through the material parameters used, $\delta^0_M$ in our case. On the other hand, some lattice dynamical properties of ionic conductors have been interpreted in the light of the bond fluctuation model mentioned in the introduction. Thus, another cause that results in the large deviation shown in Figs. 1 and 2 could be the bond fluctuation process. To separate the contributions of defects from the bond fluctuation process and other effects if any, is a subject left for a future study.
§4. Conclusion

The temperature dependences of the elastic constants of AgBr were calculated from room temperature to near the melting point through an expression derived from the Murnaghan equation of state. The comparison with the experimental data revealed that whereas $C_{44}$ exhibits good agreement, the values of $C_{11}$ and $C_{12}$ are overestimated by large amounts above 550 K. Possible origin of the deviation is discussed briefly. The result of the analysis suggests that the expression widely used in the literature to estimate the temperature dependence of the elastic constant should be used carefully.

References